

DEVELOPING GEOMETRY...

Angles in parallel lines and polygons

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What do I need to be able to do?

By the end of this unit you should be able to:

- Identify alternate angles
- Identify corresponding angles
- Identify co-interior angles
- Find the sum of interior angles in polygons
- Find the sum of exterior angles in polygons
- Find interior angles in regular polygons

Keywords

- Parallel:** Straight lines that never meet
Angle: The figure formed by two straight lines meeting (measured in degrees)
Transversal: A line that cuts across two or more other (normally parallel) lines
Isosceles: Two equal size lines and equal size angles (in a triangle or trapezium)
Polygon: A 2D shape made with straight lines
Sum: Addition (total of all the interior angles added together)
Regular polygon: All the sides have equal length; all the interior angles have equal size

Basic angle rules and notation R

Acute Angles
 $0^\circ < \text{angle} < 90^\circ$

Right Angles
 90°

Obtuse
 $90^\circ < \text{angle} < 180^\circ$

Reflex
 $180^\circ < \text{angle} < 360^\circ$

Straight Line
 180°

The letter in the middle is the angle
 The arc represents the part of the angle

Angle Notation: three letters ABC
 This is the angle at B = 113°
Line Notation: two letters EC
 The line that joins E to C

Vertically opposite angles
 Equal
Angles around a point
 360°

Parallel lines

Still remember to look for angles on straight lines, around a point and vertically opposite!

Lines OF and BE are transversals (lines that bisect the parallel lines)

Corresponding angles often identified by their "F shape" in position

Alternate angles often identified by their "Z shape" in position

This notation identifies parallel lines

Alternate/ Corresponding angles

Because alternate angles are equal the highlighted angles are the same size

Because corresponding angles are equal the highlighted angles are the same size

Co-interior angles

Because co-interior angles have a sum of 180° the highlighted angle is 110°

Os angles on a line add up to 180° co-interior angles can also be calculated from applying alternate/ corresponding rules first

Triangles & Quadrilaterals R

Side, Angle, Angle

Side, Angle, Side

Side, Side, Side

Link to steps R

Properties of Quadrilaterals

Square
 All sides equal size
 All angles 90°
 Opposite sides are parallel

Rectangle
 All angles 90°
 Opposite sides are parallel

Rhombus
 All sides equal size
 Opposite angles are equal

Parallelogram
 Opposite sides are parallel
 Opposite angles are equal
 Co-interior angles

Trapezium
 One pair of parallel lines

Kite
 No parallel lines
 Equal lengths on top sides
 Equal lengths on bottom sides
 One pair of equal angles

Sum of exterior angles

Exterior angles all add up to 360°

Using exterior angles

Interior angle + Exterior angle = straight line = 180°
 Exterior angle = $180 - 165 = 15^\circ$

Number of sides = $360^\circ \div \text{exterior angle}$
 Number of sides = $360 \div 15 = 24$ sides

Exterior Angles
 Are the angle formed from the straight-line extension at the side of the shape

Sum of interior angles

Interior Angles
 The angles enclosed by the polygon

$(\text{number of sides} - 2) \times 180$

Sum of the interior angles = $(5 - 2) \times 180$

This shape can be made from three triangles
 Each triangle has 180°

Sum of the interior angles = $3 \times 180 = 540^\circ$

Remember this is all of the interior angles added together

Missing angles in regular polygons

Exterior angle = $360 \div 8 = 45^\circ$

Interior angle = $\frac{(8-2) \times 180}{8} = \frac{6 \times 180}{8} = 135^\circ$

Exterior angles in regular polygons = $360^\circ \div \text{number of sides}$

Interior angles in regular polygons = $\frac{(\text{number of sides} - 2) \times 180}{\text{number of sides}}$